

Table 1: Almost rigorous Galerkin errors for an attracting periodic point for $\nu = 0.127$. Computed for $m = 7$, $M = 40$. The far tail is given by $2.17661e + 10/k^{12}$

k	E_n
1	[-0.000278108, 0.000278108]
2	[-0.000988331, 0.00123214]
3	[-0.00711298, 0.00711298]
4	[-0.0204183, 0.016248]
5	[-0.0578071, 0.057807]
6	[-0.0918419, 0.113116]
7	[-0.0787589, 0.0787591]

1 Galerkin errors

14.IV.2002 We computed 'almost rigorous' self-consistent bounds and Galerkin errors for them. By the Galerkin error we understand

$$E_n = Q_n F(x) - Q_n(F(P_n(x))) \quad (1)$$

where x is a point from our bounds. This number measures the influence of tail on n -th coordinate of the vector field.

By 'almost rigorous' we mean the following: we have a nonrigorous trajectory for 16-dim Galerkin projection and we use the bounds from this trajectory to initiate a construction of self-consistent bounds. We always obtain rigorous isolation for $k > m$.

It is quite clear that to obtain small Galerkin errors we need to increase m . The increase of M (with m fixed) does not give anything (compare Tables 2 and 3).

Table 2: Almost rigorous Galerkin errors for an attracting periodic point for $\nu = 0.127$. Computed for $m = 10$, $M = 30$. The far tail is given by $6.11022e + 10/k^{12}$

k	E_n
1	$[-2.3921e - 07, 2.39215e - 07]$
2	$[-1.20577e - 06, 1.17378e - 06]$
3	$[-5.99336e - 06, 5.99319e - 06]$
4	$[-2.60657e - 05, 2.68461e - 05]$
5	$[-7.67115e - 05, 7.67093e - 05]$
6	$[-0.000355372, 0.000348309]$
7	$[-0.000892646, 0.000892671]$
8	$[-0.00231196, 0.0022598]$
9	$[-0.00432135, 0.00432125]$
10	$[-0.0024444, 0.00306841]$

Table 3: Almost rigorous Galerkin errors for an attracting periodic points for $\nu = 0.127$. Computed for $m = 10$, $M = 60$. The far tail is given by $5.73671e + 12/k^{14}$

k	E_n
1	$[-2.3921e - 07, 2.39215e - 07]$
2	$[-1.20577e - 06, 1.17378e - 06]$
3	$[-5.99336e - 06, 5.99319e - 06]$
4	$[-2.60657e - 05, 2.68461e - 05]$
5	$[-7.67115e - 05, 7.67093e - 05]$
6	$[-0.000355372, 0.000348309]$
7	$[-0.000892646, 0.000892671]$
8	$[-0.00231196, 0.0022598]$
9	$[-0.00432135, 0.00432125]$
10	$[-0.0024444, 0.00306841]$

Table 4: Almost rigorous Galerkin errors for an attracting periodic point for $\nu = 0.127$. Computed for $m = 12$, $M = 36$. The far tail is given by $2.86054e + 10/k^{12}$

k	E_n
1	$[-2.04951e - 09, 2.04951e - 09]$
2	$[-1.01938e - 08, 1.00326e - 08]$
3	$[-7.18664e - 08, 7.18661e - 08]$
4	$[-2.44784e - 07, 2.4913e - 07]$
5	$[-1.04403e - 06, 1.04403e - 06]$
6	$[-4.15987e - 06, 4.07871e - 06]$
7	$[-1.12029e - 05, 1.12029e - 05]$
8	$[-4.85983e - 05, 4.92694e - 05]$
9	$[-0.000119345, 0.000119345]$
10	$[-0.000294634, 0.000299381]$
11	$[-0.000532375, 0.000532377]$
12	$[-0.000328375, 0.000274536]$

Table 5: Almost rigorous Galerkin errors for an attracting periodic point for $\nu = 0.127$. Computed for $m = 14$, $M = 42$. The far tail is given by $1.52229e + 10/k^{12}$

k	E_n
1	$[-1.42487e - 11, 1.42487e - 11]$
2	$[-1.02477e - 10, 1.02161e - 10]$
3	$[-5.55127e - 10, 5.55124e - 10]$
4	$[-1.8769e - 09, 1.89425e - 09]$
5	$[-1.11987e - 08, 1.11988e - 08]$
6	$[-3.48188e - 08, 3.44648e - 08]$
7	$[-1.36906e - 07, 1.36906e - 07]$
8	$[-5.1026e - 07, 5.16143e - 07]$
9	$[-1.34831e - 06, 1.34832e - 06]$
10	$[-5.74969e - 06, 5.70405e - 06]$
11	$[-1.36326e - 05, 1.36326e - 05]$
12	$[-3.34293e - 05, 3.30973e - 05]$
13	$[-5.77198e - 05, 5.77195e - 05]$
14	$[-2.84312e - 05, 3.19057e - 05]$

Table 6: Almost rigorous Galerkin errors for an attracting periodic point for $\nu = 0.127$. Computed for $m = 16$, $M = 48$. The far tail is given by $1.65978e + 13/k^{14}$

k	E_n
1	$[-7.72824e - 14, 7.72818e - 14]$
2	$[-7.28497e - 13, 7.22119e - 13]$
3	$[-3.09047e - 12, 3.09052e - 12]$
4	$[-1.52849e - 11, 1.52276e - 11]$
5	$[-6.95511e - 11, 6.95517e - 11]$
6	$[-2.10899e - 10, 2.13371e - 10]$
7	$[-1.17469e - 09, 1.1747e - 09]$
8	$[-3.49014e - 09, 3.44518e - 09]$
9	$[-1.31506e - 08, 1.31505e - 08]$
10	$[-4.78653e - 08, 4.85653e - 08]$
11	$[-1.23229e - 07, 1.23229e - 07]$
12	$[-5.17394e - 07, 5.12188e - 07]$
13	$[-1.20614e - 06, 1.20615e - 06]$
14	$[-2.92623e - 06, 2.89293e - 06]$
15	$[-5.06648e - 06, 5.06643e - 06]$
16	$[-2.63477e - 06, 3.00641e - 06]$